Note on congruent numbers

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A positive integer A is said to be a *congruent number* if A is the area of a right triangle with rational sides. One may consider only A square-free.

In 1998, F. R. Nemenzo [3] listed all congruent numbers less than 40 000, and non-congruent numbers were studied by F. Lemmermeyer [2] and W. Cheng and X. Guo [1] among others.

I will present short proof of the following

Theorem 1. Every positive integer A fulfilling the Diophantine equation

$$A^2 = x^2 + y^4$$

is a congruent number.

References

[1] W. Cheng, X. Guo. Some new families of non-congruent numbers, J. Numb. Theory 196 (2019), 291–305.

[2] F. Lemmermeyer. Some families of non-congruent numbers, Acta Arith. 110 (2003)

[3] F. R. Nemenzo. All congruent numbers less than 40000, Proc. J. Acad. 74 (1998), 29-31.